#### Search for the 17 MeV particle with the PADME detector



#### Paolo Valente on behalf of the PADME Collaboration





#### X17 "anomalies"

Several anomalies in angular correlations of e+ e- internally converted in the radiative disexcitation of nuclear levels excited by a proton beam observed at ATOMKI, first in the decays of <sup>8</sup>Be\*, then also <sup>4</sup>He\*, <sup>12</sup>C\* [and even in the Giant-Dipole Resonace]

Interpreted with a **new particle** of mass:

<sup>8</sup>Be:  $M_x = (16.70 \pm 0.35_{stat} \pm 0.5_{syst}) \text{ MeV}$ <sup>4</sup>He:  $M_x = (16.94 \pm 0.12_{stat} \pm 0.21_{syst}) \text{ MeV}$ <sup>12</sup>C:  $M_x = (17.03 \pm 0.11_{stat} \pm 0.20_{syst}) \text{ MeV}$ 

of mass  $M_x$  in a  $N^* \rightarrow N X_{17}$  transition

Observed also at HUS (Vietnam) in the <sup>8</sup>Be\* with a different setup [Universe 2024, 10(4)]

[PRL 116 (2016) 042501]



[PR C 104 (2021) 044003] [PR C 106, L061601 (2022)]



 $\theta_{\min} \sim asin(\frac{M_X}{M_{N_H}-M_N}); M_X = (16.85 \pm 0.04) \text{ MeV}; \chi^2 = 17.3, \text{ ndf} = 10, P(\chi^2) = 7\%$ The rate measurements indicate  $\Gamma(N^* \rightarrow N X_{17}) / \Gamma(N^* \rightarrow N g) \sim 5 \times 10^{-6}$ 

**Angular excesses** approx. consistent with being due to a particle



[PRD108, 015009 (2023)]:





#### Ongoing experimental initiatives Recent result from MEG II arXiv:2411.07994

Measurement on <sup>7</sup>Li target to reproduce <sup>8</sup>Be ATOMKI result, <u>no signal found</u> ULs on  $\Gamma(^{8}\text{Be}^{*} \rightarrow ^{8}\text{Be } X(\text{ee})) / \Gamma(^{8}\text{Be}^{*} \rightarrow ^{8}\text{Be } \gamma)$  for 17.6, 18.1 MeV transitions

```
MEG-II result still compatible at 1.5 \sigma with the ATOMKI combination i.e. M<sub>X</sub> = 16.85(4) MeV JHEP 04 (2025) 035
```

#### Further iniatives:

- AN2000 electrostatic accelerator at INFN LNL [In data taking]
- At n\_TOF EAR2 neutron line at CERN [2025 proposal]
- Tandem accelerator in Montreal [JPC Ser. 2391 (2022) 012008]
- Van de Graaf accelerator at IEAP Prague [NIM A 1047 (2023) 167858]









#### Search for a resonance on a thin target

$$\sigma_{res} \propto \frac{g_{V_e}^2}{2m_e} \pi Z \, \delta(E_{res} - E_{beam})$$

- $\sigma$  goes with  $\alpha_{em} \rightarrow dominant process$  wrt other pair production processes ( $\alpha_{em}^2, \alpha_{em}^3$ )
- $\sqrt{s}\,$  as close as possible to expected mass

 $\rightarrow$  expected **enhancement** in  $\sqrt{s}$  over the SM background

Fine scan the e<sup>+</sup> beam energy around the resonance [E<sub>e+</sub>~283 MeV]
 → measure two-body final state yield N<sub>2</sub> for each energy point

N<sub>2</sub>(s) = N<sub>POT</sub>(s) × B(s) if only "background", i.e. SM contribution

to be compared with:

 $N_2(s) = N_{POT}(s) \times [B(s) + S(s; M_X, g) \times \epsilon_S(s)]$ 



- S(s; M<sub>x</sub>, g) signal per POT for given {mass, coupling} = {M<sub>x</sub>, g}
- ε<sub>s</sub>(s) signal acceptance and selection efficiency



## Search for a resonance on a thin target

- If **X17** decays to e+e- pairs, it should also be produced in **e+e- annihilations**
- The basics of a resonance search are discussed in PRD 106 (2022) 115036
- Focus on a **Vector state interpretation** for brevity:

 $\mathcal{L}^{\text{Vect.}} \supset \sum_{f=e,u,d} X^{\mu}_{17} \bar{f} \gamma_{\mu} (g_{vf} + \gamma^5 \tilde{g}_{vf}) f.$ 



- The resonance is much narrower wrt the **momentum spread** of the positron **beam**
- Not negligible broadening due to the electron binding energy











## 2022 setup



Run I and II dedicated to dark photon searches with associated production

#### In 2022 PADME setup specifically adapted for Run-III:

- Active target: polycrystalline diamond [0.1 mm thick]
- No magnetic field [PADME dipole off]
- Calorimeter: 616 BGO crystals, 21x21x230 mm<sup>3</sup> each
- New scintillating bar hodoscope in front of calorimeter for elγ
- Timepix silicon detector array for beam spot monitoring
- Lead-glass beam catcher (OPAL/NA62 LAV)









#### Run III data set



#### Actually two interleaved scans, 1.5 MeV step

Nearby energy points acquired 1.5 months apart









#### **Signal selection**

- Selection algorithm as independent as possible on the beam variations:
- Retune beam center run by run with an error << mm
- Overall, make marginal use of the cluster reconstructed energy





Selected events 4% background













# **Analysis scheme**

Rewrite the yield formula as:

$$\frac{N_2(s)}{N_{POT}(s) B(s)} = 1 + \frac{S(s; MX, g) \varepsilon_S(s)}{B(s)}$$
  
R(s)

R(s)=1 if only SM **"background"**, but different effects can lead to a **deviation** from above: **K(s)** 

Question: is R(s) more consistent with

• K(s) or

• K(s) × 
$$\left[1 + \frac{S(s; MX, g) \epsilon_{S}(s)}{B(s)}\right]$$
?



MC with  $M_X = 16.8 \text{ MeV}$ ,  $g_V = 8 \times 10^{-4}$ 









## **Error budget:** N<sub>2</sub>, **B**

Source	Error on N <sub>2</sub> [%]	
Statistics	~0.6	30k events /energy point
Background subtraction	0.3	using <b>angular side-bands</b> (Bremsstrahlung, 4%)
Total	0.65	

Source	Error on B [%]	Monte Carlo + data-driven checks	in the scale K(s), e.g.: Absolute cross section (rad. corr. at 3%)			
MC statistics	0.40		+ data-driven target thickness (known 4%)			
Data/MC efficiency	0.35		Source	Correlated B error [%]		
(Tag&Probe)			Below res. statistics	0.40		
Cut stability	0.04		Below res.	1.80		
Beam spot variations	0.05		acceptance; s slope			
Total	0.54		Total	1.85		
		4		SERVIPHYSICAL SOCIETICS		







Common systematic errors on **B** enter

# **Error budget: N**<sub>POT</sub>

Source	Error on N <sub>POT</sub> [%]	
Statistics, ped subtraction	negligible	
Energy scale from BES	0.3	<b>BES</b> from Timepix beam spot $\sigma_{x}$
Error from rad. induce slope	Variable, ~0.35	
Total	0.45	

Source	Common error on N <sub>POT</sub> [%]	
pC / MeV	2.0	[ <i>JHEP</i> 08 (2024) 121]
Energy loss, data/MC	0.5	
Rad. induced loss, constant term	0.3	
Total	2.1	







### **Analysis scheme: S**

Analysis compares R(s) to  $K(s) \times [1 + S(s; M,g_v) \epsilon/B]$ 

Expected signal **yield** from points taken from **PRL 132 (2024) 261801**, including effect of **motion of the atomic electrons** in the diamond target from Compton profiles

- Parameterized **S vs E\_{beam}** with a **Voigt function**:
- Convolution of the Gaussian BES with the Lorentzian
- OK in the core within % with some dependence on BES
- Uncertainty in the curve parameters as nuisances:
- Peak yield: 1.3%
- Lorentzian width around resonance energy: 1.72(4) MeV
- Relative BES: 0.025(5)%









#### **Analysis scheme: ε/B**

Analysis compares R(s) to  $K(s) \times [1 + S(s; M,g_v) \epsilon/B]$ 

Efficiency ε determined from MC: large cancellation of systematic errors using ε/B

Fit **ɛ/B(s<sup>1/2</sup>)** with a **straight line**, include **fit parameters as nuisances** 



- Separate fits for scan 1 and scan 2, mutually compatible
- Reproduced with MC







### **Possible scale effects, K(s)**

#### **Radiative corrections** evaluated using **Babayaga**, ee( $\gamma$ ) and $\gamma\gamma(\gamma)$



The scaling with the below resonance is affected by a -1.5(1.5)% shift because of radiative corrections, but the expected total error covers for it:  $1.8\%(B) + 2.1\%(N_{PoT}) = 2.8\%$ 

Insertion of Babayaga-generated events in the MC (up to 10  $\gamma$ 's)  $\rightarrow$  no effect on  $\epsilon$ 







#### **Analysis scheme: expected sensitivity**

- Evaluate expected 90% CL upper limit in absence of signal
- Define Q statistic based on likelihood ratio:  $Q = L_{S+B}(g_v, M_X) / L_B$
- The likelihood includes terms for each nuisance parameter pdf
- For a given  $M_X$ , CLs =  $P_s$  / (1  $P_B$ ) is used to define the UL on  $g_v$



Probabilities  $P_s$  and  $P_B$  obtained using **simulations**, where the observables are always sampled, with **nuisance parameters** fixed to the B and S+B fits



In presence of a **signal**, the expected limit is weaker, e.g. for  $M_X = 16.9 \text{ MeV}$ ,  $g_{ve} = 5 \times 10^{-4}$ 



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For details: arXiv:2503.05650 [accepted by JHEP]



# The "blind unblinding" procedure

To validate the error estimate applied procedure described in 2503.05650 [hep-ex]

#### Define a **side-band** in R(s), **excluding 10 energy points** of the scan in a **blind way**

#### Masked periods defined by optimizing the probability of a linear fit in $\sqrt{s}$

- 1. Threshold on the  $\chi^2$  fit in side-band is  $P(\chi^2) = 20\%$ , corresponding to reject 10% of the times
- 2. If passed, check if the **fit pulls** are **Gaussian**
- 3. If passed, check if a straight-line fit of the pulls has **no slope in s**<sup>1/2</sup> (within 2 sigma)
- 4. If passed, check if constant term and slope of the linear fit for K(s) are within two sigma of the expectations, i.e.: +/- 4.8% for the constant, (-0.6 +/- 1.2) % MeV<sup>-1</sup> for the slope

#### Successfully applied:

- 1.  $P(\chi^2) = 74\%$
- 2. Pulls Gaussian fit probability 60%
- 3. Slope of pulls consistent with zero
- 4. Constant term = 1.0116(16), Slope = (-0.010 +- 0.005) MeV<sup>-1</sup>

At 90%CL additional errors <1% Proceed to box opening







# **Box opening**

#### **Excess** is observed **beyond** the $2\sigma$ coverage (2.5 $\sigma$ local)

At  $M_x = 16.90(2)$  MeV,  $g_{ve} = 5.6 \times 10^{-4}$ , the global probability dip reaches  $3.9_{-1.1}^{+1.5}$  %

Corresponding to (1.77  $\pm$ 0.15)  $\sigma$  one-sided (look-elsewhere calculated exactly from the toy pseudo-events)

A second excess is present at ~ 17.1 MeV, but the absolute probability there is ~ 40%

If a  $3\sigma$  interval is assumed for observation following the estimate  $M_x = 16.85(4)$  of PRD 108, 015009 (2023), the p-value dip deepens to  $2.2_{-0.8}^{+1.2}$ % corresponding to (2.0±0.2)  $\sigma$  one-sided

17



#### For details: ArXiv:2505.24797 [hep-ex]



# **Box opening**

Check the data distribution vs likelihood fit

to evaluate  $Q_{obs}(S+B)$ 

Fit probability is 60%











# **Box opening**



For comparison, check **expected UL bands bkg-only** vs **B+S(16.9 MeV, 5 × 10**<sup>-4</sup>)



M<sub>x</sub> (MeV)

18

18.5





16

16.5

17

17.5

### **PADME Run IV optimized setup**

New data set being acquired to better clarify:

• set the target closer to the calorimeter, increase acceptance









#### **Run IV – new tracking detector**

New detector for Run IV [Frascati, Napoli, Roma]:

- ATLAS micromegas-based tracker to separately measure the absolute cross sections of ee/γγ
- Improvement in angle resolution, also provides beam spot





Two 5 cm gaps, can operate in TPC mode

Resistive circuit (common, 3 HV zones)







# **Run IV assumptions**

Improvements wrt Run III:

- Increase acceptance: allow even safer treatment for edge effects
- Increase **monitoring** power and **redundancy**: better stability
- Alternative flux determinations:  $\gamma\gamma$ , new end of line monitor, target, chamber
- Increase statistics: 1.5×10<sup>10</sup> POT per energy point

Expectations for Run IV:

- ×2 acceptance increase
- ×2 statistics increase
- 2.5 days for data collection, 3000 e<sup>+</sup>/spill as in Run III
- Points divided into 2 scans as in Run III









Source	Unc	ertainty [%]	Note	
	Run III	Run IV		
N <sub>2</sub>	0.6	0.3	Uncorrelated	
N <sub>PoT</sub>	0.35	0.3	Uncorrelated	
В	0.55	0.3	Uncorrelated	
Total on g <sub>R</sub>	0.89	0.5	Uncorrelated	



## Conclusions

The "X<sub>17</sub>" excess remains not confirmed but not disproved No SM explanation viable The PADME experiment is in a favorable condition to clarify

Data from 4×10<sup>11</sup> e<sup>+</sup> on target used for resonance search in the mass region 16.4 –17.4 MeV with a blind analysis

**Overall uncertainties of 0.9% on 40+ points have been obtained** 

No indication of  $X_{17}$  with global p-values well beyond  $2\sigma$ 

An excess at 16.90 MeV: local p-value 2.5  $\sigma$ , global 1.77(15)  $\sigma$ A new data taking with an upgraded detector is ongoing: Jun-Nov 2025, possible extension beginning of 2026







#### **Additional material**







# **Run-III concepts – the signal selection**

Select any two-body final state (ee,  $\gamma\gamma$ ) with both daughters in ECal acceptance:

- 1. Fix R<sub>Max</sub> at Ecal, away from Ecal edges
- 2. Given s, derive R<sub>Min</sub>, E<sub>Min</sub>, E<sub>Max</sub>
- 3. Select cluster pairs:
  - With Energy >  $E_{min} \times 0.4$
  - In time within 5 ns
  - Clus1: In ( $R_{min}$  D,  $R_{max}$ ), D = 1.5 L3 crystals
  - Clus2: R > R<sub>min</sub>- D
- 4. Select pairs back-to-back in the c.m. frame

Rmax chosen to be away from Ecal edges by more than the size of 1 BGO crystal cell for any period in the data set





1 □ = 1 BGO crystal = 21.5 x 21.5 mm







## Details on expected background: s dependence

Expected background B determined from MC, stat error per period:  $\delta B \sim 4 \times 10^{-3}$ Fit of B(s<sup>1/2</sup>) with a straight line (only including statistical errors here)



Fit mode	P0 [10 <sup>-6</sup> ]	P1 [10 <sup>-7</sup> / MeV]	Corr	Fit prob
Only scan1	3.549(3)	3.71(10)	0.12	75%
Only scan2	3.567(4)	3.96(13)	-0.19	31%
All periods	3.558(2)	3.85(8)	-0.008	9%

Background curve slightly depend on the scan

Considered in alternative analysis (see later)







# **Box opening – III Other checks**

Checked other sensitivity methods

#### Perform the automatic procedure but fit with a constant:

Re	sult:	Ori	ginal version:
1.	$P(\chi^2) = 37\%$	1.	$P(\chi^2) = 74\%$
2.	Pulls gaussian fit prob > 30%	2.	Pulls gaussian fit probability > 45%
3.	Slope of pulls consistent with zero	3.	Slope of pulls consistent with zero
4.	Constant = 1.0112(14)	4.	Constant = 1.0116(16), Slope = (-0.010 +- 0.004 ) MeV <sup>-1</sup>

The center of the masked region does not change: 16.888 MeV The excess also remains basically of the same strength:  $1.6\sigma$ 

Use scan1-scan2 separate parametrizations for B(s) instead of using B(s) / point: Excess region only slightly affected and equivalent to ~1.6  $\sigma$ 



# **Box opening – IV Check of correction**

After box opening, can check ageing correction applied, slope was 0.097(7) Fully consistent (observed excess alters only marginally)



The slope has been used to correct for the radiation-induced effect, acting as a separate nuisance

Again no significant change in the location of the excess and in the global p-value



#### Details on the event count N<sub>2</sub>

**Background** subtraction using side-bands (bremsstrahlung, ~4%) Correction relative variation +-1%, statistical uncertainty on  $\delta N_2 \sim 0.3\%$ 



# Details on background: cut stability

Check if MC and data yields stable vs  $R_{\text{min}},\,R_{\text{max}}$  (edge effects, leakage)

Vary  $R_{max}$  by +-2  $E_{Cal}$  cells around nominal cut of 270 mm: 230 mm  $\rightarrow$  300 mm



Stability is observed within a coverage band of +-0.2%, add 0.035% uncorrelated systematic error on B





## Details on background: acceptance variations

The selection makes use of the expected beam direction, from the spot measured at the diamond target and the center of gravity (COG) of 2 body final states at ECal

Systematic shifts in the COG position translate into acceptance systematic errors

Largest effect in y due to acceptance limitations (rectangular magnet bore) Fractional variations range from 0.08% to 0.1% mm<sup>-1</sup> for s<sup>1/2</sup> from 16.4 to 17.4 MeV

An error of 1 mm in the COG is a conservative estimate  $\rightarrow$  systematic error < 0.1%





### **Details on background: cluster reconstruction**

من 300 من 100 م

300

100

-100

Efficiency

0.95 MC true

0.9

0.85

0.75

Efficiency around 1 within few % except in specific regions (Ecal edges, dead cells)

Tag & probe: method-induced bias 2.3(2)%, stable along the data set

Data/MC method efficiency stable along the data set and at the few per mil



# Details on background: cluster reconstruction

**Check of reconstruction efficiency:** 

Efficiency for data and MC evaluated using tag-and-probe technique Statistical error dominated by background subtraction at tag level

Data/MC energy-flat, compatible with 1, error O(1%) per period

<Data/MC> vs period, P<sub>Fit</sub>(const) ~ 20%

No correction applied per period, statistical-systematic error of 0.35%





↩

# What's PADME – the detector: beam monitors

 $1.5 \times 1.5 \text{ mm}^2$  spot at active, 100  $\mu$ m diamond target: position, multiplicity  $1 \times 1 \text{ mm}^2$  pitch X,Y graphite strips [NIM A 162354 (2019)]







CERN MBP-S type dipole: 112×23 mm<sup>2</sup> gap, 70 cm long Beam monitor (Si pixels, Timepix3) after bending:  $\sigma_P/P_{beam} < 0.25\%$ 







#### What's PADME – the TDAQ concepts

Three trigger lines: Beam based, Cosmic ray, Random

Trigger and timing based on custom board [2020 IEEE NSS/MIC, doi: 10.1109/NSS/MIC42677.2020.9507995]

Most detectors acquired with Flash ADC's (CAEN V1742), O(10<sup>3</sup>) ch's: 1 μs digitization time window 1 V dynamic range, 12 bits sampling rates at 1, 2.5, 5 GS/s

Level 0 acquisition with zero suppression, ×10 reduction  $\rightarrow$  200 KB / ev. Level 1 for event merging and processing, output format ROOT based

First experiment goal (A' invisible search) required 10<sup>13</sup> POT, O(80 TB)

## Details on the flux N<sub>POT</sub>: leakage correction

Loss from detailed MC vs vertical position checked against data in test beam Very good data-MC agreement, correction 1.2%, systematic error 0.5% Significant period-by-period variation of the correction: -4% to +2%



### **Details on the flux N<sub>POT</sub>: rad-induced correction**

The literature indicates possible changes in SF57 transparency for O(krad) Estimate of Run-III dose: 2.5 krad

Estimated from 3 flux proxy observables: Qx target, <E<sub>Ecal</sub>>, period multiplets

Leadglass yield decreases with relative POT slope of 0.097(7) Constant term uncertainty of 0.3% added as scale error Slope error included in POT uncertainty



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# Measurement of $e^+e^- \rightarrow \gamma\gamma$ : data set and concept

Using < 10% of Run II data,  $N_{POT} = (3.97 \pm 0.16) \times 10^{11}$  positrons on target Expect  $N_{ee \rightarrow \gamma\gamma} \sim 0.5$  M, statistical uncertainty < 1% Include various intensities, e<sup>+</sup> time profiles for systematic studies Evaluate efficiency corrections from MC + data

Master formula:



 $N_{POT}$  from diamond active target

Uncertainty on e<sup>-</sup> density  $n_{e/S} = \rho N_A Z/A d$  depends on thickness d

Run #	NPOT [10 <sup>10</sup> ]	e <sup>+</sup> /bunch [10 <sup>3</sup> ]	length [ns]
30369	8.2	$27.0 \pm 1.7$	260
30386	2.8	$19.0 \pm 1.4$	240
30547	7.1	$31.5 \pm 1.4$	270
30553	2.8	$35.8 \pm 1.3$	260
30563	6.0	$26.8 \pm 1.2$	270
30617	6.1	$27.3 \pm 1.5$	270
30624	6.6	$29.5 \pm 2.1$	270
30654	No-target	$\sim 27$	$\sim 270$
30662	No-Target	$\sim 27$	$\sim 270$







# $e^+e^- \rightarrow \gamma\gamma$ : POT, target thickness

 $N_{POT}$  from active target, uncertainty is 4%:

- 1. Absolute calibration by comparing with lead-glass calorimeter fully contained from 5k to 35k e+/bunch
- 2. When focusing beam into 1-2 strips, non-linear effects observed

 $n_{e/S}$  from target thickness, uncertainty is 3.7% (i.e., ~3.7  $\mu$ m)

- 1. Measured after assembly with profilometer with 1  $\mu m$  resolution as difference with respect to the supporting surface
- 2. Correction due to roughness (quoted as 3.2  $\mu m$  by producer): compare precision mass and thickness measurements on similar diamond samples







## The blind unblinding procedure: details



Constant term and slope of the optimized fit estimate the true values for K(s) Results of the procedure ran on toy experiments with constant = 1, slope = 0



Moreover the procedure correctly finds the central location of signals when present

## The PCL method

Using CLsb but clipping to the median every downward fluctuation of the limit



The global p-value is only slightly affected, consistent with the coverage modifications of this method







## The PADME ECal

#### The main detector for the signal selection [JINST 15 (2020) T10003]:

- 616 BGO crystals, 2.1 x 2.1 x 23 cm<sup>3</sup>
- BGO covered with diffuse reflective TiO<sub>2</sub> paint + 50–100 μm black tedlar foils (optical isolation)







#### Calibration at several stages:

- BGO + PMT equalization with <sup>22</sup>Na source before construction
- Cosmic-ray calibration using the MPV of the spectrum
- Temperature monitoring + scale correction data driven

# The PADME beam catcher calorimeter

The main detector for the flux determination [JHEP 08 (2024) 121]:

- SF57 block, reused from OPAL, tested for the NA62 LAV detector [JINST 12 (2017) 05, P05025]
- Several testing campaigns
  - A few positrons
  - O(2000) PoT cross-calibration with the BTF FitPix





# The blind unblinding constraining power

Determine the number of times an experiment outcome would be rejected in presence of additional uncorrelated errorsx

- With the cut applied, errors > 1% are excluded at 90% CL
- Had we put a tighter condition, we would have excluded additional errors at 0.8% but at the cost of risking to reject by statistical fluctuations ~8% of the outcomes





#### The new micromega-based tracker

#### Detector installed with the novel diamon-shaped readout

Outer dimensions 88 x 88 cm<sup>2</sup>

Readout by APV25

Time window up to 675 ns (drift time ~500 ns)

Gas mixture: Ar:CF<sub>4</sub>:Isobutane = 88:10:2

Provides beam spot with uncertainty  $\sigma_{\text{x},\text{y}}$  ~ 30  $\mu\text{m}$ 

Track points with  $\sigma_{x,y} \sim 350 \ \mu m$  and  $\sigma_z \sim 2 \ mm$  per point



